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An Optimal Model and Production Planning in Upholstery by Linear Integer Programming

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Authors' contributions

This work was carried out in collaboration between both authors. Both authors read and approved the final manuscript.

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Abstract

This research effort used an upholstery factory as a case study to apply the idea of integer programming for an ideal model. In order to allocate limited and readily available material resources to competing products (Bed (6x6ft), Bed (6x4ft), Wardrobe (6x6ft), Wardrobe (6x4ft), Side Drawer, and Shoe Rack) in the furniture factory with a view to maximizing profit, the Revised Simplex method of solving linear programming and the branch and bound method of solving integer programming models were used in this study. The analysis was carried out with the help of the LINDO software version 6.1 using data containing the availability of materials, sales volume for each of the product types, machine and time it takes to complete the manufacturing process of each product type, as well as profit per unit of the product as collected from the factory. The outcome indicated that 38 units of the Bed (6x6ft), 10 units of the Wardrobe (6x4ft), and 0 units of the other products needed to be manufactured to make a monthly profit of no more than \$1711700. From the result, it was observed that the Wardrobe (6x4ft) and Bed (6x6ft) contributed majorly to the profit, hence the recommendation that more of the Wardrobe (6x4ft) should be produced and sold for optimum profit.



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1 Introduction

Every organization, business, or enterprise strives to be profitable since doing so ensures its ongoing existence and productivity. Concerns regarding the dissolution or liquidation of organizations have grown over time; this may be due to a lack of profitable growth that is both effective and sustainable.

Profit is the main driver of people entering the business world, thus businesses can only develop and expand when they are making money. In the labor market, a lot has been done to secure profit maximization in Nigeria, ranging from rigorous adherence to the mathematical or economic concepts of profit maximization to stringent enforcement of worker layoffs, which is an anti-people attitude. Even while it sounds wonderful, the latter has proven difficult for businesses and organizations to achieve, leading many to downsize their workforces or retrench employees as a quick fix.

Growing rates of organizational liquidation have slowed the nation's economic growth by increasing unemployment or underemployment. Our youth are experiencing high unemployment rates, social vices have risen, and young people are turning to illicit means of making a living. All of these are actually a result of businesses and organizations closing down that would have given these young people productive employment and contributed to the country's gross domestic product (GDP). This is a result of businesses making bad decisions.

The linear programming method is one of the ways to guarantee profit maximization that has been mathematically demonstrated. A mathematical method for choosing how to allocate a company's limited resources to best achieve a goal is known as linear programming (LP). Additionally, it is a mathematical strategy applied in Operation Research (OR) or Management Sciences to resolve certain issues like allocation, transportation, and assignment issues that allow for a choice or options amongst potential solutions Yahya [1].

In accordance with a predetermined standard for optimality, linear programming is "a mathematical technique useful for allocating scarce or limited resources to several competing activities." Sharma [2].

There are differing views on whether linear programming techniques should be used in various management decision-making processes as a result of continual advancement in the application of these approaches to realworld business challenges over a lengthy period of time. Since it is simpler to find the best use of scarce resources in developing economies, linear programming is a crucial tool for resource allocation. A Soviet mathematician named Leonid Kantorovich, who introduced the concept of linear programming to the Soviet Union in 1939, developed strategies for dealing with complex linear programming issues, such as the method of using the dual problem's optimal solution to solve the primal problem. He created the now-famous mathematical method of linear programming in 1939, a few years before Dantzig did [3]. He used LP to organize the varied activities of the U.S. Air Force related with the issue of supplies to the Force and to solve practical challenges. Because LP modeling works to achieve a single target of either maximizing (profit or contribution) or minimization, Charles et al. [4] referred to it as a single objective optimization strategy. (cost or time). According to Gupta and Hira [5], LP modeling can be used to optimize a linear function known as the objective function, which is dependent on an assembly of constraint functions. According to Dowing [6], linear programming is far better to alternative optimization approaches like the Lagrangian method and Graphic method. Lagrangian approach. In agreement with Turban and Meredith [7], Dwivedi [8] claimed that one of the most well-known management science tools is linear programming. The majority of scholars Wagner [9] and Lucey [10] studied the idea that linear programming is a method used in operations research. They believe that it is one of the most commercially successful operations research applications, with Wagner [9] stating that there is strong evidence to suggest that it has the greatest economic impact. Kareem and Aderoba [11] used data from a cocoa processing plant in Akure, Ondo State, Nigeria, to demonstrate the efficiency of the linear programming model in maintenance and personnel planning. Marek [12] addresses the problem of supply chain management in the foundry industry. In order to determine the highest profit from the manufacture of soft drink at the Nigeria Bottling Company, Ilorin facility, Balogun et al. [13] applied the linear programming method. By using the software linear interactive optimizer (LINDO) to maximize the profit of the Khadi and Village Industries

Commission (KVIC) connected to servodaya Sangham, Murugan and Manivel [14] attempted to illustrate the usage of linear programming technique. The concept of the revised simplex technique with sensitivity analysis was used to Kingmos Paints Nig. Ltd. by Ikpang et al. in [15]. Abdennour [16] used linear programming approach to model to elaborate the optimal production plan. In order to calculate the best profit for the well-known neighborhood bakery Shukura Bakery in Zaria, Kaduna State, Nigeria, Zakariyya et al. [17] used the linear programming technique.

However, there is no assurance that an integer valued solution will be obtained while solving an LP model. A non-integer valued solution, for instance, will have no importance when determining how many beds and wardrobe would be needed to produce in order to maximize profit. It is not possible to arrive at the best solution by rounding off to the nearest integer. In these situations, integer programming is employed to guarantee that the decision variables have integer values.

Thus, the revised simplex method is a commonly used algorithm for solving linear programming problems, including profit maximization problems.

This work demonstrates the pragmatic use of linear programming methods in maximization of profit at the Mudiame Business Concept Enterprise.

The purpose of this study is to apply integer linear programming to the Mudiame commercial enterprise in order to maximize profits, as well as to determine the optimal linear model for the company's products and the product mix that will maximize profits for the firm.

2 Brief Background on the Case Study

Mudiame Business Concept Enterprise is a business-based organization with a number of production facilities that is housed within the Mudiame University neighborhood in Irrua, Esan Central, Edo State, Nigeria. It was created to conduct business operations involving the production of items, the processing of raw materials, and the delivery of sales and services within her many sections. The study focused only on the furniture factory out of the several industrial sectors that exist, including water production, bakery and pastry making, soap making, fashion and design, and furniture manufacturing. The sector was created in an effort to fill the gap left by the high, medium, and low classes' lack of access to basic necessities. Its manufacturing is primarily focused on providing the common people with the necessities. The furniture factory produces six different items: Side Drawer, Shoe Rack, Wardrobe (6x6ft x 4ft), Bed (6x6ft x 6ft), and Wardrobe (6x6ft x 4ft). As a result, choosing the number combinations of the products produced is a crucial and significant management choice.

3 Methodology/ Method of Data Analysis

The financial statement that includes the total production for one month was the tool used for this study project. The Mudiame Business Concept Enterprise, Irrua, Edo State, total production and sales volumes for one month were used in the study.

The study's methodology is the conventional maximizing problem's revised simplex method. The regular simplex method, which is a modified version of the simplex method, may not be practical for really big issues because it requires a lot of memory space to store the simplex when using a computer. The procedure needs only;

- The net evaluation row Δ_j to determine the non-basic variable that enters the basis.
- The pivot column
- The current basis variables and their values (X_B column) to determine the minimum positive ratio and then identify the basis variable to leave the basis.

Revised Simplex Method is an efficient computational procedure for solving an LPP with less labour. In this method, we need not to compute all the value of X_B , Y_j and $Z_j - C_j$ at each iteration. The core computation is rooted in the basis *B* and its inverse B^{-1} The inverse of the next basis is computed directly from the current

basis without actually inverting the next basis. The current basis inverse and the original data of the problem are used to determine the entering and departing vectors.

3.1 Revised simplex method in standard forms

Standard form I: In this form, an identity matrix is assumed to be obtained after introduction of

In order to solve LP problem using revised simplex method, the objective function is also considered as one of the constraints equation in which value of Z can be made as large as possible and unrestricted in sign. Thus, the set of constraints can be written as:

 $Z - c_1 x_1 - c_2 x_2 - \dots - c_n x_n - 0. x_{n+1} - 0. x_{n+2} - \dots - 0. x_{n+m} = 0$ $a_{11} x_1 + a_{12} x_2 + \dots + a_{1n} x_n + x_{n+1} = b_1$ $a_{21} x_1 + a_{22} x_2 + \dots + a_{2n} x_n + x_{n+2} = b_2$ $\vdots \qquad \vdots \qquad \vdots$ $a_{m1} x_1 + a_{m2} x_2 + \dots + a_{mn} x_n + x_{n+m} = b_m \qquad . \qquad . \qquad .$ $x_1, x_2 \cdots x_{n+m} \ge 0$ (1)

In matrix notations, the system of equation above can be expressed as Z - Cx = 0

 $\begin{array}{l}Ax = b\\x \ge 0\end{array}$

And in the system of equation (1), there are (m + 1) simultaneous linear equations in (n + m + 1) variables $(Z, x_1, x_2, ..., x_{n+m})$. The aim now is to solve equation (1) such that Z is as large as possible and unrestricted in sign, subject to the condition $x_1, x_2, ..., x_{n+m} \ge 0$. By rewriting equation (1) in more symmetric notations as follows, we get:

 $1. x_0 + a_{01}x_1 + a_{02}x_2 + \dots + a_{0n}x_n + a_{0,n+1}x_{n+1} - a_{0,n+2}x_{n+2} - \dots - a_{0,n+m}x_{n+m} = 0$ $0. x_0 + a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n + x_{n+1} = b_1$ $0. x_0 + a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n + x_{n+2} = b_2$ $0. x_0 + a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mn}x_n + x_{n+m} = b_m$

Where $Z = x_0$ and $-c_j = a_{0j}$ (j = 1, 2, ..., n + m). In matrix notations it may be written as

$$\begin{bmatrix} 1 & a_{01} & a_{02} & \cdots & a_{0n} & a_{0,n+1} & \cdots & a_{0,n+m} \\ 0 & a_{11} & a_{12} & \cdots & a_{1n} & 1 & \cdots & 0 \\ 0 & a_{21} & a_{22} & \cdots & a_{2n} & 0 & \cdots & 0 \\ \vdots & \vdots \\ 0 & a_{m1} & a_{m2} & \cdots & a_{mn} & 0 & \cdots & 1 \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ \vdots \\ x_{n+m} \end{bmatrix} = \begin{bmatrix} 0 \\ b_1 \\ b_2 \\ \vdots \\ b_m \end{bmatrix}$$
Or
$$\begin{bmatrix} 1 & a_0 \\ 0 & A \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ \vdots \\ x_{n+m} \end{bmatrix} = \begin{bmatrix} 0 \\ b_1 \\ b_2 \\ \vdots \\ b_m \end{bmatrix}$$
(2)

Where, $a_0 = (a_{01}, a_{02}, \dots, a_{0,n+m})$

4 Data Presentation, Analysis and Result Interpretation

The source of the information for this study was Mudiame Business Concept Enterprise in Irrua, Edo State. The information includes the maximum amount of raw materials that can be used for manufacturing, the profit contribution per piece of furniture produced, and the amount of each resource used to make one piece of furniture.

The Table1 below contains the data as it was acquired.

Resources		Product					
	x_1	x_2	x_3	x_4	x_5	x_6	resources
Labour (hr) (LB)	4.0	4.0	7.0	4.0	1.5	1.0	192
Machinery/Diesel (hr) (MC)	1.25	1.25	3.50	1.33	0.58	0.58	96
Wood (pcs) (WD)	2.50	2.00	6.00	2.50	0.25	0.25	240
Edge Tape (roll) (ET)	0.25	0.20	0.27	0.15	0.05	0.05	25
3x30 Screw Nails (pkt) (SN 1)	0.25	0.25	0	0	0.15	0.15	30
5x30 Screw Nails (pkt) (SN 2)	0.25	0.25	0	0	0	0	20
Bed Hook (pair) (BH)	1	1	0	0	0	0	74
3x16 Screw Nails (pkt) (SN 3)	0	0	0.3	0.2	0	0	18
Bracket Iron (pkt) (BI)	0	0	0.25	0.25	0.17	0.17	15
Wardrobe Handles (pcs) (WHD)	0	0	8	2	1	0	386
Wardrobe Hinges (pair) (WHG)	0	0	6	3	0	0	220
Drawer Runner (pair) (DR)	0	0	2	0	1	0	145
Back Cover (pcs) (BC)	0	0	2	1	0.25	0.25	52
Unit Profit	33400	28700	72500	44250	8000	8500	

Table 1. Data on raw material mix per item

Where x_1 : Bed (6x6ft),

 x_2 : Bed (6x4ft),

 x_3 : Wardrobe (6x6ft),

 x_4 : Wardrobe (6x4ft),

 x_5 : Side Drawer,

 x_6 : Shoe Rack.

By taking into account the objective function as one of the constraints and, if necessary, adding the slack and excess variables to the inequalities in order to transform them into equalities, we state the provided issue in the revised simplex form. LINDO software will be used for the data analysis. (Version 6.1).

5 Model Formulation

The model is given as:

Maximize $Z = \sum_{j=1}^{6} p_j x_j$ Subject to $= \sum_{j=1}^{6} a_{ij} x_j \le b_i$ $x_j \ge 0, j = 1, ..., 6, i = 1, 2, ..., 13$

where Z is the objective function.

 x_i represents the types of furniture to be produced.

 p_i represents the profit contribution per furniture produced.

 b_i represents the maximum values for the production constraints

The Linear Programming Model formulated is thus:

Maximize $Z = 33400x_1 + 28700x_2 + 72500x_3 + 44250x_4 + 8000x_5 + 8500x_6$

Subject to

 $\begin{array}{ll} 4.0x_1 + 4.0x_2 + 7.0x_3 + 4.0x_4 + 1.5x_5 + 1.0x_6 \leq 192 & \text{(Labour Constraints)} \\ 1.25x_1 + 1.25x_2 + 3.50x_3 + 1.33x_4 + 0.58x_5 + 0.58x_6 \leq 96 & \text{(Machinery/Diesel Constraints)} \\ 2.50x_1 + 2.00x_2 + 6.00x_3 + 2.50x_4 + 0.25x_5 + 0.25x_6 \leq 240 & \text{(Wood Constraints)} \end{array}$

25 (Edge Tape Constraints) (3x30 Screw nail Constraints)
(5x30 Screw nail Constraints) (Bed Hook Constraints) (3x16 Screw Nail Constraints) (Bracket Iron Constraints) (Wardrobe Handles Constraints) (Wardrobe Hinges Constraints)
(Drawer Runner Constraints) (Back Cover Constraints)

5.1 Solution of Lpp using revised simplex method

By introducing the slack variables in the objective functions above we have and putting the problem clearly in standard form, we have that:

 $Z - 33400x_1 - 28700x_2 - 72500x_3 - 44250x_4 - 8000x_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_4 + 0s_5 - 8500x_6 + 0s_1 + 0s_2 + 0s_3 + 0s_5 + 0s_$ $+ 0s_6 + 0s_7 + 0s_8 + 0s_9 + 0s_{10} + 0s_{11} + 0s_{12} + 0s_{13} = 0$ $4.0x_1 + 4.0x_2 + 7.0x_3 + 4.0x_4 + 1.5x_5 + 1.0x_6 + s_1 = 192$ $1.25x_1 + 1.25x_2 + 3.50x_3 + 1.33x_4 + 0.58x_5 + 0.58x_6 + s_2 = 96$ $2.50x_1 + 2.00x_2 + 6.00x_3 + 2.50x_4 + 0.25x_5 + 0.25x_6 + s_3 = 240$ $0.25x_1 + 0.20x_2 + 0.27x_3 + 0.15x_4 + 0.50x_5 + 0.50x_6 + s_4 = 25$ $0.25x_1 + 0.25x_2 + 0.15x_5 + 0.15x_6 + s_5 = 30$ $0.25x_1 + 0.25x_2 + s_6 = 20$ $x_1 + x_2 + s_7 = 74$ $0.3x_3 + 0.2x_4 + s_8 = 18$ $0.25x_3 + 0.25x_4 + 0.17x_5 + 0.17x_6 + s_9 = 15$ $8x_3 + 2x_4 + x_5 + s_{10} = 386$ $6x_3 + 3x_4 + s_{11} = 220$ $2x_3 + x_5 + s_{12} = 145$ $2x_3 + x_4 + 0.25x_5 + 0.25x_6 + s_{13} = 52$ And $x_1, x_2, x_3, x_4, x_5, x_6, s_1, s_2, \dots, s_{13} \ge 0$

Step 1: Define/Identify the original column vector (P_n) and the coefficient matrix C_n of the objective row.

									$P_n =$	=									
[P ₁	P_2	P_3	P_4	P_5	P_6	P_7	P_8	P_9	$P_{10}^{'}$	P_{11}	P_{12}	P_{13}	P_{14}	P_{15}	P_{16}	P_{17}	P_{18}	P ₁₉ 7	
<i>x</i> ₁	x_2	x_3	x_4	x_5	x_6	S_1	S_2	S_2	S_3	S_4	S_5	S_6	S_7	S_8	S_9	S_{10}	S_{11}	<i>s</i> ₁₂	
4.0	4.0	7.0	4.0	1.5	1.0	1	0	0	0	0	0	0	0	0	0	0	0	0	
1.25	1.25	3.50	1.33	0.58	0.58	0	1	0	0	0	0	0	0	0	0	0	0	0	
2.50	2.00	6.00	2.50	0.25	0.25	0	0	1	0	0	0	0	0	0	0	0	0	0	
0.25	0.20	0.27	0.15	0.50	0.50	0	0	0	1	0	0	0	0	0	0	0	0	0	
0.25	0.25	0	0	0.15	0.15	0	0	0	0	1	0	0	0	0	0	0	0	0	
0.25	0.25	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	
1	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	
0	0	0.3	0.2	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	
0	0	0.25	0.25	0.17	0.17	0	0	0	0	0	0	0	0	1	0	0	0	0	
0	0	8	2	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	
0	0	6	3	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	
0	0	2	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1	0	
L 0	0	2	1	0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	1 J	
	[33400			2500	4425		800	-	8500										
Z = [3	33400	2870	00 72	500	44250	8	000	85	00	0 0	0	0 0	0	0 () ()	0	0 0	0]	

Step 2: Calculate the new value of column vector (P'_n) for the non-basic variables and the X_B which is the RHS column vector. $P'_n = B^{-1} * P_n$ where B^{-1} is the inverse of original column of basic variables and P_n is the original value of the column vector.

Step 3: Identify the new basic variable (if exists) by calculating the (C'_n) value for non-basic variables. $C'_n = C_n - C_B * P'_n$ where Cn' is the new value of coefficient of objective row; C_n is the original value of coefficient of objective function; C_B is the value of coefficient of Basic variable in the objective row. Any C'_n that has the smallest value is the New Entering Variable.

That is, $C'_1 = C_1 - C_B * P'_1, C'_2 = C_2 - C_B * P'_2, C'_3 = C_3 - C_B * P'_3$ and so on.

Step 4: Finding the exiting row using the (X'_B) and the new value of the (P'_n) by calculating the ratio of the corresponding elements. The one with the smallest positive value is the leaving variable.

$$X_{B} = \begin{bmatrix} 192\\96\\240\\25\\30\\20\\74\\18\\15\\386\\220\\145\\52 \end{bmatrix} = X'_{B} = B^{-1} * X_{B}$$

Step 5: Repeat Step 2, 3, 4 until no other new basic variables can be identified.

The LINDO software is employed in solving the problem and the underlying algorithm in LINDO is Revised Simplex Method.

6 Result from Lindo

LP OPTIMUM FOUND AT STEP 3

OBJECTIVE FUNCTION VALUE

1) 1634868.

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VARIABL	E VALUI	E REDUCED COST
X1	37.928570	0.000000
X2	0.000000	4682.856934
X3	0.000000	29429.714844
X4	2.500000	0.000000
X5	0.000000	4664.285645
X6	30.285715	0.000000
Х	0.000000	5442.143066

ROW SLACK OR SURPLUS DUAL PRICES

2)	0.000000	8328.571289
3)	27.698572	0.000000
4)	131.357147	0.000000
5)	0.000000	342.857147
6)	15.975000	0.000000
7)	10.517858	0.000000
8)	36.071430	0.000000
9)	17.500000	0.000000
10)	9.226429	0.000000
11)	0.000000	5442.143066
12)	386.000000	0.000000
13)	212.500000	0.000000
14)	145.000000	0.000000
15)	41.928570	0.000000

Fig. 1. The report window in LINDO showing optimum solution

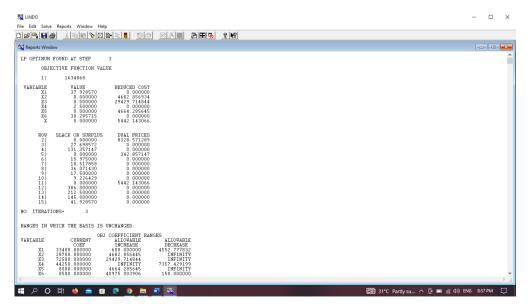


Fig. 2. The report window in LINDO showing optimum solution continued

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30.285715

The solution shows that X1 = 37.928570

X4 = 2.500000 X6 =

Since we cannot introduce or produce fraction of bed, integer programming will be introduced by applying branch and bound technique to have a new problem of

Maximize Z=33400x1+28700x2+72500x3+44250x4+8000x5+8500x6

Subject to

4.0x1 + 4.0x2 + 7.0x3 + 4.0x4 + 1.5x5 + 1.0x6 < 192	(Labour Constraints)
1.25x1+1.25x2+3.50x3+1.33x4+0.58x5+0.58x6 < 96	(Machinery/Diesel Constraints)
2.50x1+2.00x2+6.00x3+2.50x4+ 0.25x5+0.25x6 <240	(Wood Constraints)
0.25x1+0.20x2+0.27x3+0.15x4+0.50x5+0.50x6 < 25	(Edge Tape Constraints)
0.25x1+0.25x2+ 0.15x5+0.15x6 <30	(3x30 Screw nail Constraints)
0.25x1+0.25x2 <20	(5x30 Screw nail Constraints)
x1+x2 <74	(Bed Hook Constraints)
0.3x3+0.2x4 <18	(3x16 Screw Nail Constraints)
0.25x3+0.25x4+ 0.17x5+0.17x6 <15	(Bracket Iron Constraints)
8x3+2x4+x5 < 386	(Wardrobe Handles Constraints)
6x3+3x4 <220	(Wardrobe Hinges Constraints)
2x3+x5 <145	(Drawer Runner Constraints)
2x3+x4+0.25x5+0.25x6 <52	(Back Cover Constraints)
X1 <= 37	

Solving gives

LP OPTIMUM FOUND AT STEP 1

OBJECTIVE FUNCTION VALUE

1) 2124000.

VARIAB	LE VALU	UE REI	DUCED COST
X1	0.000000	10850.000	000
X2	0.000000	15550.000	000
X3	0.000000	4937.5000	000
X4	48.000000	0.00000	00
X5	0.000000	8593.7500	000
X6	0.000000	2562.5000	000
ROW	SLACK OR	SURPLUS	DUAL PRICES
2)	0.000000	11062.5000	00
3)	32.160000	0.00000)
4)	120.000000	0.00000	0
5)	17.799999	0.00000	0
6)	30.000000	0.00000)
7)	20.000000	0.00000	0
8)	74.000000	0.00000	0
9)	8.400000	0.000000)
	3.000000	0.00000)
11)	290.000000	0.0000	00
12)	76.000000	0.00000	0
13)	145.000000	0.0000	00
,	4.000000	0.00000	0
,	37.000000	0.00000	0
,			

Fig. 3. The report window in LINDO showing optimum solution for the first integer programming constraint

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OBJECTIVE FUNCTION VALUE	
1) 2124000.	
VARIABLE VALUE REDUCED COST X1 0.00000 10550.000000 X2 0.00000 15550.00000 X3 0.00000 1937.50000 X4 48.00000 0.00000 X4 48.00000 0.00000 X5 0.00000 8537.550000 X6 0.000000 2562.50000	
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Fig. 4. The report window in LINDO showing optimum solution for the first integer programming constraint continued

The solution shows that X4 = 48

So, we check for additional constraint x1 > 38, and applying branch and bound technique that gives a new problem of

Maximize Z=33400x1+28700x2+72500x3+44250x4+8000x5+8500x6

Subject to

```
(Labour Constraints)
4.0x1 + 4.0x2 + 7.0x3 + 4.0x4 + 1.5x5 + 1.0x6 < 192
1.25x1+1.25x2+3.50x3+1.33x4+ 0.58x5+0.58x6 <96 (Machinery/Diesel Constraints)
                                                           (Wood Constraints)
2.50x1+2.00x2+6.00x3+2.50x4+ 0.25x5+0.25x6 <240
0.25x1+0.20x2+0.27x3+0.15x4+0.50x5+0.50x6 < 25
                                                      (Edge Tape Constraints)
0.25x1 + 0.25x2 + 0.15x5 + 0.15x6 < 30
                                                              (3x30 Screw nail Constraints)
0.25x1+0.25x2 <20
                                                           (5x30 Screw nail Constraints)
                                                                  (Bed Hook Constraints)
x1+x2 <74
0.3x3+0.2x4 <18
                                                            (3x16 Screw Nail Constraints)
0.25x3 + 0.25x4 + 0.17x5 + 0.17x6 < 15
                                                                (Bracket Iron Constraints)
                                                            (Wardrobe Handles Constraints)
8x3+2x4+x5 < 386
                                                            (Wardrobe Hinges Constraints)
6x3+3x4 <220
2x3+x5 < 145
                                                            (Drawer Runner Constraints)
                                                              (Back Cover Constraints)
2x3+x4+ 0.25x5+0.25x6 <52
X1 > 38
```

Solving gives

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LP OPTIMUM FOUND AT STEP 1

OBJECTIVE FUNCTION VALUE

1) 1711700.

VARIABLE VALUE REDUCED COST

X1	38.000000	0.000000
X2	0.000000	15550.000000
X3	0.000000	4937.500000
X4	10.000000	0.000000
X5	0.000000	8593.750000
X6	0.000000	2562.500000

ROW SLACK OR SURPLUS DUAL PRICES

2)	0.000000	11062.500000	
3)	35.200001	0.000000	
4)	120.000000	0.000000	
5)	14.000000	0.000000	
6)	20.500000	0.000000	
7)	10.500000	0.000000	
8)	36.000000	0.000000	
9)	16.000000	0.000000	
10)	12.500000	0.000000	
11)	366.000000	0.000000	
12)	190.000000	0.000000	
13)	145.000000	0.000000	
14)	42.000000	0.000000	
15)	0.000000	-10850.000000	

Fig. 5. The report window in LINDO showing optimum solution for the 2nd integer programming constraint

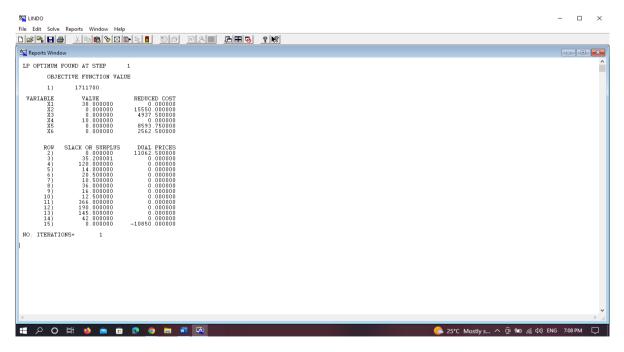


Fig. 6. The report window in LINDO showing sensitivity analysis

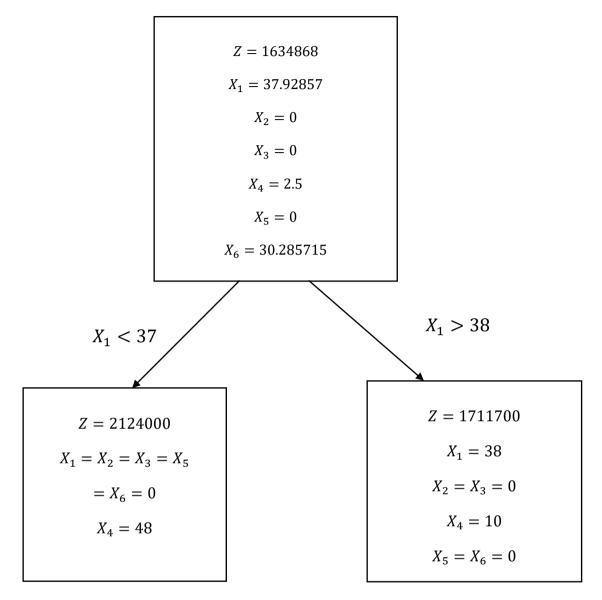


Fig. 7. integer results using branch and bound

7 Result Interpretation

From Figs. 1 and 2, the optimum value is obtained after the third iteration, producing an optimum profit of N1634868.; and that 37.92857 x_1 : Bed (6x6ft), 2.5 (x_4) wardrobes (6x4ft), and 30.285715 x_6 : Shoe Rack contribute to the maximum profit of N1634868monthly.

Since, there are fractions in the results, the concept of branch and bound method of solving integer programming is introduced. This yield the results in Figs. 3 and 4 respectively.

The out come of the whole integer programming is represented in Fig. 5 which gave both optimal solution and fathomed solution.

Thus, Fig. 5 optimum solution shows that optimal solution of \aleph 1711700 will be reached only when the company produces only 38 pieces of x_1 , and 10 pieces of x_4 in the mix without producing x_2x_3 , x_5 and x_6 .

8 Summary, Conclusion and Recommendation

8.1 Summary

The objective of this study was to apply linear programming in obtaining the product mix for the furniture production process of Mudiame Business Concept Enterprise. The decision variables in this research work are the six different types of furniture (bed (6x6ft), bed (6x4ft), wardrobe (6x6ft), wardrobe (6x4ft), side drawer, shoe rack) produced by the factory. The researcher focused mainly on thirteen resources (labour, machinery, wood, edge tape, screw nails, bed hook, bracket iron, wardrobe handles, wardrobe hinges, drawer runner, back cover) used in the production and the amount of resource required of each variable (furniture). The result shows that 38 units of the Bed (6x6ft), 10 units of Wardrobe (6x4ft), and 0 units for the rest of the products should be produced to yield a maximum profit of \aleph 1711700 monthly [18-21].

8.2 Conclusion

Based on the analysis carried out in this study and the results shown, Mudiame Business Concept Enterprise should produce the six different furniture in order to satisfy her customers. Also, more of the Bed (6x6ft), and Wardrobe (6x4ft), should be produced in order to attain a maximum profit, because it contributes mostly to the profit earned by the company.

Competing Interests

Authors have declared that no competing interests exist.

References

- [1] Yahya WB. Determination of optimum product mix at minimum raw material cost, using linear programming. Nigerian Journal of Pure and Applied Sciences. 2004;19:1712-1721.
- [2] Sharma JK. Operations research; theory and applications, 3rd edition. India: Macmillan, Indian Ltd. New Delhi; 2008.
- [3] Dantzig G. Computational algorithm of the revised simplex methods. RAND Memorandum RM-1266; 1993.
- [4] Charles, Cooper, Henderson. An introduction to linear programming. John Willy, NewYork; 1963.
- [5] Gupta PK, Hira DS. Operations Research. S. Chand Company Limited, New Delhi; 2009.
- [6] Dowing ET. Theory and problems of introduction to mathematical economics. Schaum's Outline Series, McGraw-Hall Inc, New York; 1992.
- [7] Turban J, Meredith T. Principles of management science. Prentice Hall and India Private Ltd; 1991.
- [8] Dwivedi D. Managerial economics. VIKAS Publishing House PVT Limited, New Delhi; 2008.
- [9] Wagner H. Principles of operations research with application to managerial decision. Prince-Hall of India Private Limited, New Delhi; 2007.
- [10] Lucey T. Quantitative techniques. Bookpower, London; 2002.
- [11] Kareem B, Aderoba A. Linear programming based effective maintenance and manpower planning strategy. International Journal of the Computer, the Internet and Management. 2008;16:26-34.

- [12] Marek Krynke. Application of linear programming in supply chain management in the foundry metal 2020. Brno, Czech Republic, EU; 2020.
- [13] Balogun OS, Jolayemi ET, Akingbade TJ, Muazu HG. Use of linear programming for optimal production in production line in coca-cola bottling company, Illorin. International Journal of Engineering Research and Application. 2012;2(5):2004-2007.
- [14] Murugan N, Manivel S. Profit planning of an NGO run enterprises using linear programming approach. International Research Journal of Finance and Economics. 2009;23:443-454.
- [15] Ikpang NI, Itoro MT, Ekemini UG, Ekom-Obong JO, Daniel ET. Application of revised simplex method for profit maximization in a paint company. Researchjournali's Journal of Mathematics. 2021;8(2). ISSN 2349-5375.
- [16] Abdennour Hebal. Application of linear programming in production management: A case study in SOFAMEC Khenchela. Journal of Management and Economic Sciences Prospects. 2021;50N°: 50:477-495.
- [17] Zakariyya A, Mashina MS, Lawal Z. Application of linear programming for profit maximization in shukura bakery. Dutse Journal of Pure and Applied Sciences. 2022;8:1a.
- [18] Akpan NP, Iwok IA. Application of Linear Programming for Optimal Use of Raw Materials in a Bakery. International Journal of Mathematics and Statistics Invention. 2016;4:51-55.
- [19] Hillier FS, Lieberman GJ. Introduction to operations research. McGraw-Hill, New York; 2001.
- [20] Leonid K. The mathematical method of production planning and organization. Princeton University Press; 1939.
- [21] Zaman H, Rizwan F, Muhammad BT, Syed U, Naeem U, Sehrish K. Application of linear programming for profit maximization: a case of paints company. International Journal of Management Sciences and Business Research. 2016;5(12):144-151.

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